

# ECS455 Chapter 2

## Cellular Systems

### 2.2 Co-Channel Interference

**Office Hours:**

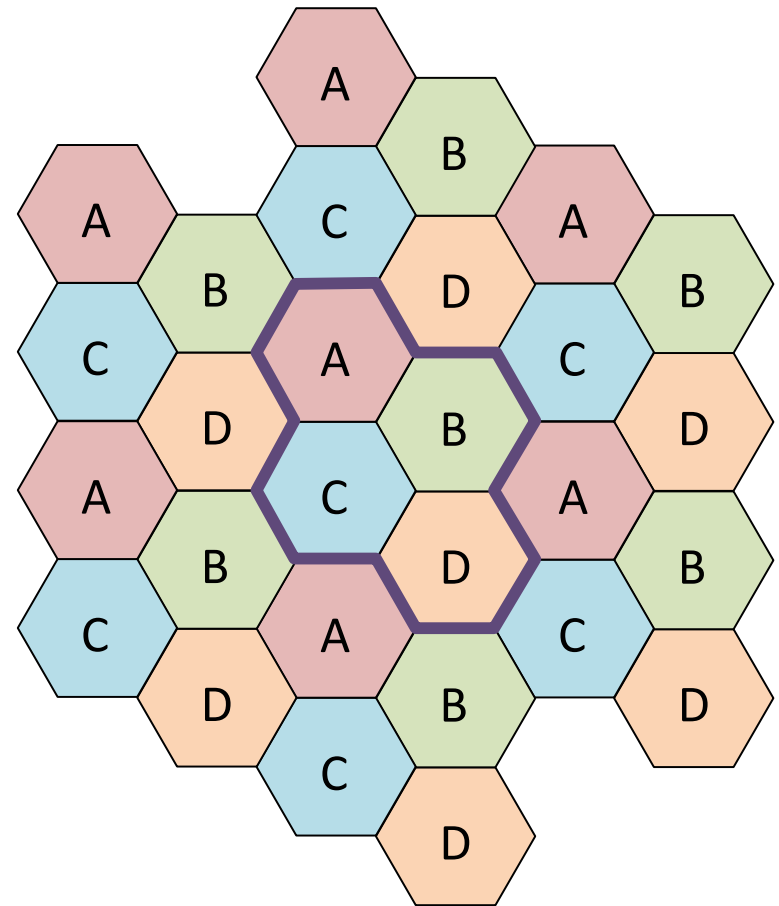
**BKD 3601-7**

**Tuesday 15:00-16:00**

**Friday 14:00-16:00**

# Co-Channel Interference

- Frequency reuse  $\rightarrow$  co-channel interference
- Consider only nearby interferers.
  - Power decreases rapidly as the distance increases.
- In a **fully equipped hexagonal-shaped** cellular system, there are always  $K = 6$  cochannel interfering cells in the **first tier**.



# Review: Simplified Path Loss Model

$$\frac{P_r}{P_t} = K \left( \frac{d_0}{d} \right)^\gamma \rightarrow P_r = \frac{P_t K d_0^\gamma}{d^\gamma} \propto \frac{1}{d^\gamma}$$

- $K$  is a unitless constant which depends on the antenna characteristics and the average channel attenuation
- $d_0$  is a reference distance for the antenna far-field
  - Typically 1-10 m indoors and 10-100 m outdoors.
- $\gamma$  is the **path loss exponent**.
  - 2 in free-space model
  - 4 in two-ray model [Goldsmith, 2005, eq. 2.17]


Captures the essence of signal propagation without resorting to complicated path loss models, which are only approximations to the real channel anyway!

Environment	$\gamma$ range
Urban macrocells	3.7-6.5
Urban microcells	2.7-3.5
Office Building (same floor)	1.6-3.5
Office Building (multiple floors)	2-6
Store	1.8-2.2
Factory	1.6-3.3
Home	3

[Goldsmith, 2005, Table 2.2]

# SIR (S/I): Definition/Calculation

- $K = \#$  co-channel interfering cells
- The **signal-to-interference ratio** (S/I or SIR) for a mobile receiver which monitors a *forward channel* can be expressed as

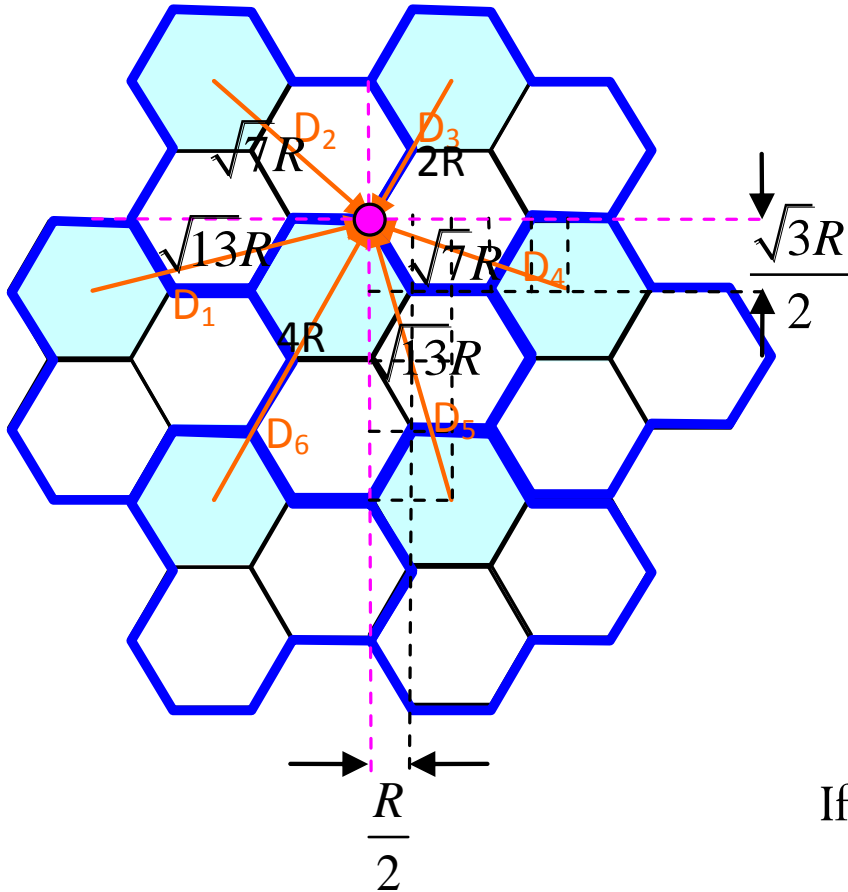
$$\text{SIR} = \frac{S}{I} = \frac{S}{\sum_{i=1}^K I_i}$$


- $S =$  the desired signal **power** from the desired base station
- $I_i =$  the interference **power** caused by the  $i$ th interfering co-channel cell base station.

# SIR Thresholds

- The SIR should be greater than a specified threshold for proper signal operation.
- In the 1G **AMPS** system, designed for voice calls, the desired performance threshold is SIR equal to **18 dB**.
- For the 2G digital AMPS system (D-AMPS or IS-54/136), a threshold of 14 dB is deemed suitable.
- For the **GSM** system, a range of **7–12 dB**, depending on the study done, is suggested as the appropriate threshold.

SIR:  $N = 3$



$$SIR = \frac{S}{\sum_i I_i} \leftarrow \text{Worst-case}$$

$$P_r = \frac{k}{d^\gamma} = k d^{-\gamma}$$

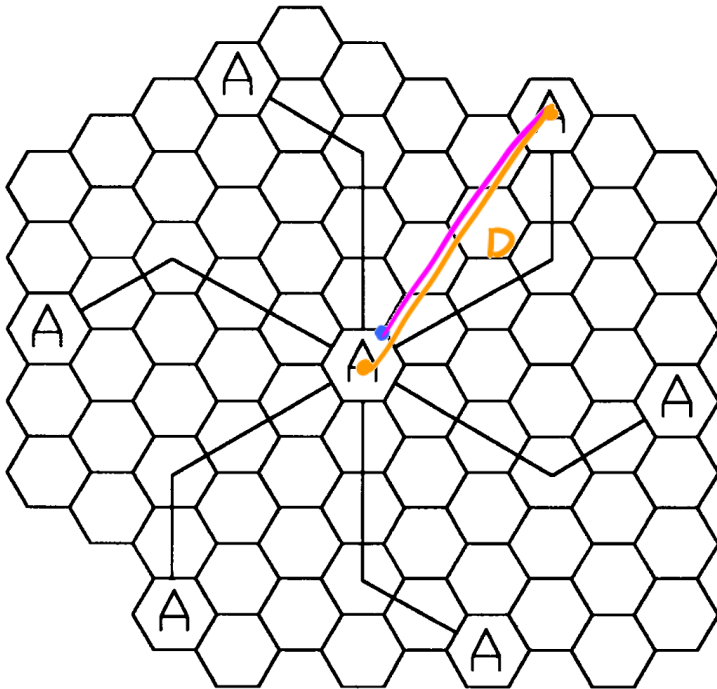
$$SIR = \frac{k/R^{\gamma}}{\sum_i k/D_i^{\gamma}}$$

$$= \frac{1}{2(\sqrt{7})^{-\gamma} + 2(\sqrt{13})^{-\gamma} + 2^{-\gamma} + 4^{-\gamma}}$$

If  $N = 19$ , will the SIR be better or worse?

larger.

# Crude Approximation



$$\text{SIR} = \frac{k/R^{\gamma}}{\sum_i k/D_i^{\gamma}} = \frac{1}{\sum_i 1/\left(\frac{D_i}{R}\right)^{\gamma}}$$

- ① Consider only 1<sup>st</sup> tier.
  - ② Worst-case distance
  - ③  ~~$D_i$~~  →  $D$  = center-to-center distance btw closet interfering cells.
- } same as previous calc.

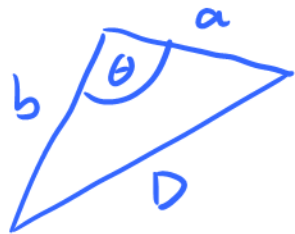
# Center-to-center distance (D)

$N \rightarrow i, j$

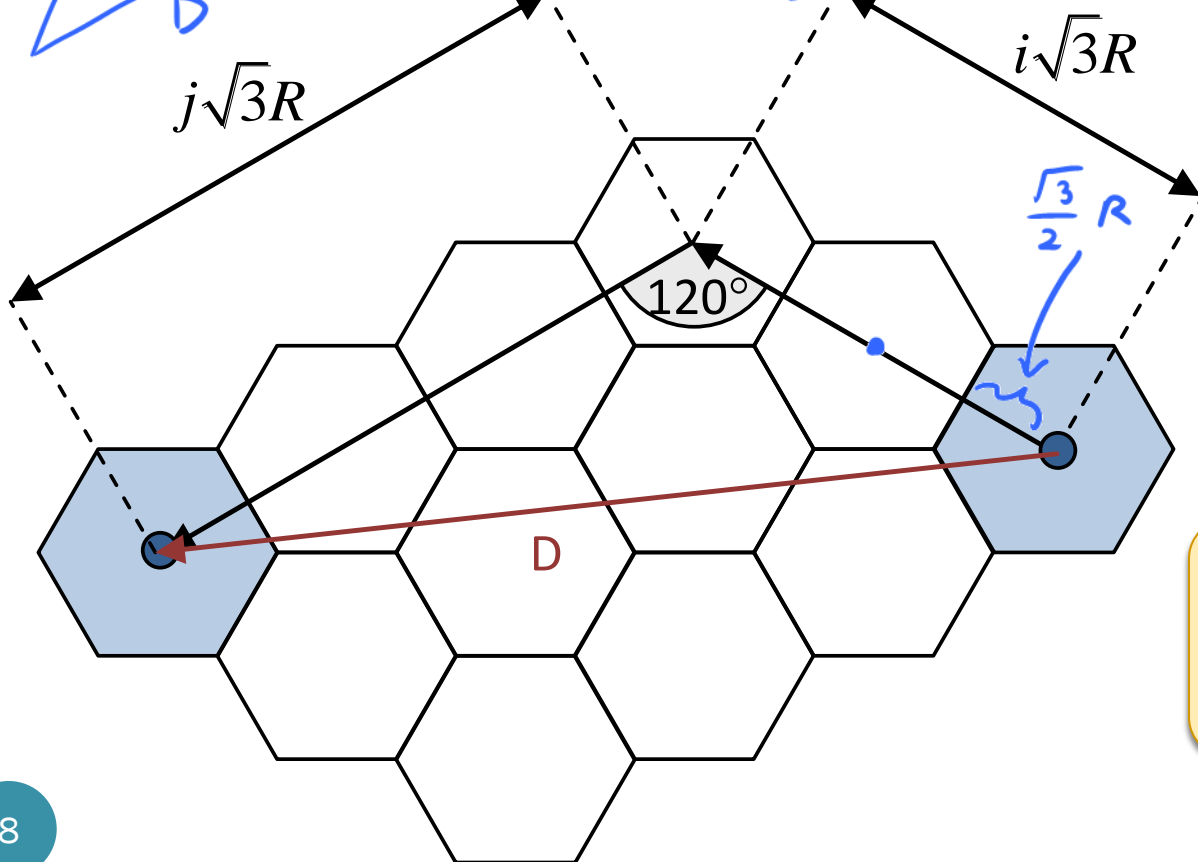
$$D = \sqrt{(i\sqrt{3}R)^2 + (j\sqrt{3}R)^2 - 2(i\sqrt{3}R)(j\sqrt{3}R)\cos(120^\circ)}$$

$$= R\sqrt{3(i^2 + j^2 + ij)} = R\sqrt{3N}$$

$-1/2$



$$D^2 = a^2 + b^2 - 2ab\cos\theta$$



This distance,  $D$ , is called **reuse distance**.

Co-channel reuse ratio

$$Q = \frac{D}{R} = \sqrt{3N}$$



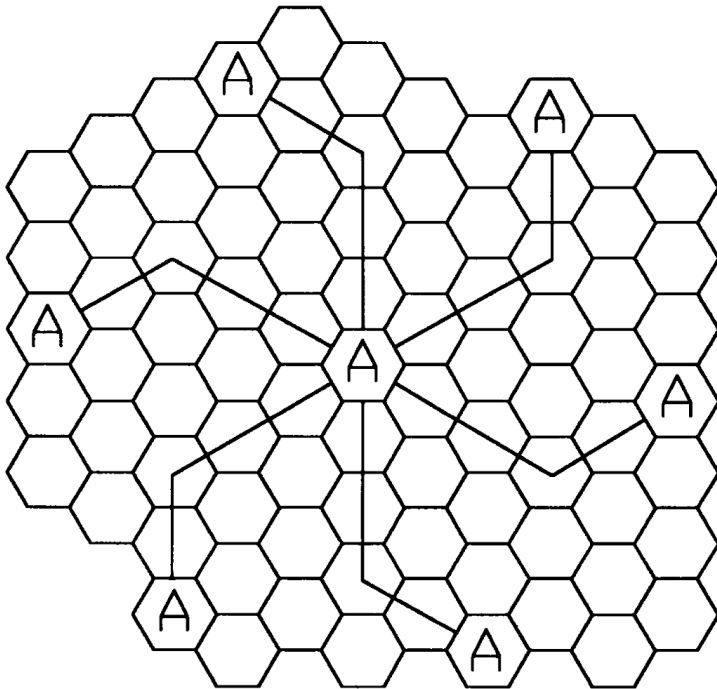
# Q and N

Co-channel reuse ratio

$$Q = \frac{D}{R} = \sqrt{3N}.$$

	Cluster Size ( $N$ )	Co-channel Reuse Ratio ( $Q$ )
$i = 1, j = 1$	3	3
$i = 1, j = 2$	7	4.58
$i = 0, j = 3$	9	5.20
$i = 2, j = 2$	12	6

# Approximation: Crude formula



$$\begin{aligned}
 \text{SIR} &= \frac{\cancel{K}/R^{+\gamma}}{\sum_i \cancel{K}/D_i^{+\gamma}} = \frac{1}{\sum_i 1/\left(\frac{D_i}{R}\right)^{+\gamma}} \\
 &\approx \frac{1}{\underset{6}{K}/\left(\frac{D}{R}\right)^{+\gamma}} = \frac{1}{K} \left(\frac{D}{R}\right)^{\gamma} \\
 &= \frac{1}{K} \left(\sqrt{3N}\right)^{\gamma} = \frac{1}{K} \left(3N\right)^{\frac{\gamma}{2}}
 \end{aligned}$$

# Summary

frequency  
FDD

$S$  = total # available duplex radio channels for the system



Frequency reuse with **cluster size  $N$**

“Capacity”

$$C = \frac{A_{\text{total}}}{A_{\text{cell}}} \times \frac{S}{N}$$

Tradeoff

$$\frac{S}{I} \approx \frac{kR^{-\gamma}}{K \times (kD^{-\gamma})} = \frac{1}{K} \left( \frac{D}{R} \right)^\gamma = \frac{1}{K} \left( \sqrt{3N} \right)^\gamma$$

↑  
the ability  
to handle  
simultaneous  
\* of calls.

→  $m$  = # channels allocated to  
each cell.

This is only  $\frac{1}{2}$  of the story!!

Quantity

vs.

Quality

# SIR: $N = 7$

$\gamma = 4$

$$SIR = \frac{1}{6} (\sqrt{3 \times 7})^\gamma$$

More accurate calculation...

$$\frac{S}{I} \approx \frac{R^{-4}}{2(D-R)^{-4} + 2(D+R)^{-4} + 2D^{-4}}$$

$$\frac{S}{I} \approx \frac{1}{2(Q-1)^{-4} + 2(Q+1)^{-4} + 2Q^{-4}}$$

